

# Experimental validation of loudspeaker equalization inside car cockpits

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## Abstract

This paper deals with the definition of an automatic tool to develop digital equalization systems for car cockpits. The main purpose is to design a digital audio processor suitable for any car compartment, whose programming parameters can be computed with a development tool, which relies only on standard acoustic measurements performed in the target car cockpit. Experimental results of the defined tools are presented using as target a Fiat Lancia Delta.

## 1 Introduction

Sound reproduction within a car inside is a difficult task. Reverberation, reflections, echo, noise and vibration are some of the issues to account for. A first step in the direction of increasing sound comfort is that of equalizing the acoustic pressure response in the frequency domain. To accomplish this task the inversion of the measured Sound Pressure Level (SPL) should be performed [1], [2]. The main target of the equalization procedure is to increase sound comfort at the driver position, option which does not directly results in an homogeneous quality in the whole car cockpit.

The constraints to be accounted for are the quality of the input signal, for instance produced by a CD player, and the computational capability of the DSP to be used in real-time as the hardware platform. Moreover the quality and the resolution of the equalization must be tailored to human earing system sensitivity. In fact it is ineffective to improve sounds in the range of frequencies which the human ears cannot sense, or to perform a too accurate correction. Therefore only listening tests can be an objective evaluation procedure of the equalization system designed.

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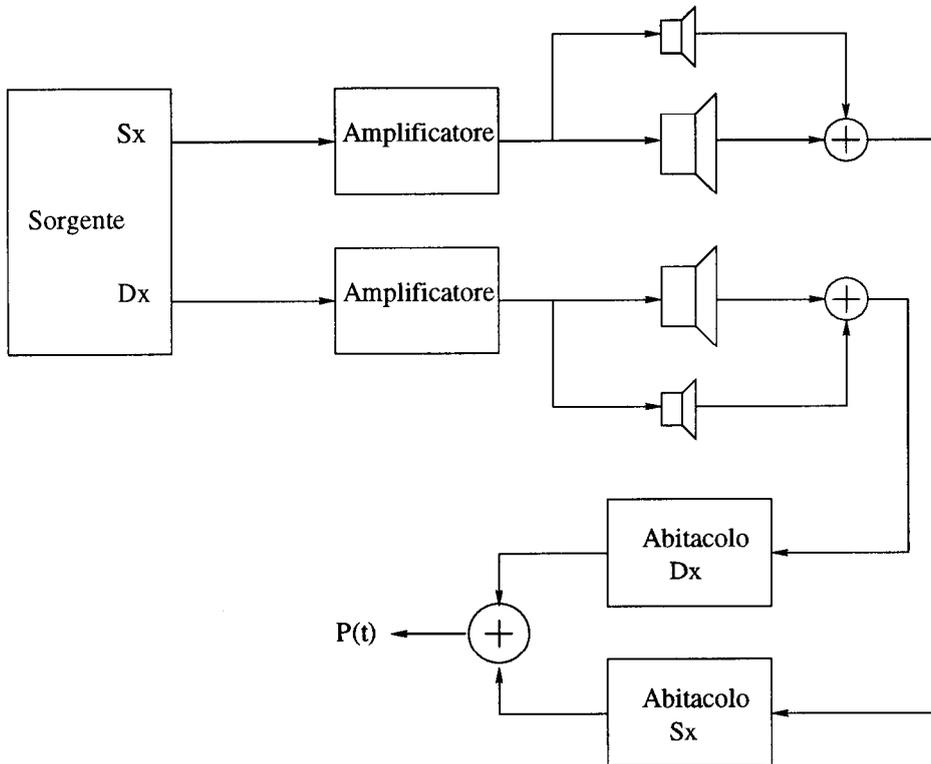


Figure 1: Hi-fi car system.

Another desired feature of the tool to be designed is its generality. The procedure should be independent of both target environment and of the instrumentation used to perform acoustic measurements. The proposed procedure relies on automatic tools which elaborate the acoustic measurements and implement the filter structure and produce the suitable coefficients for the adopted hardware platform. In this paper the results presented are obtained for a Fiat Lancia Delta, using acoustic measurements performed with AURORA [3].

The following items will be detailed in the paper.

1. Choice of the suitable car audio system and analysis of the problems related with the measurements set-up.
2. Software tools for the elaboration of measurements data, and for the computation of the filter coefficients.
3. Design of the equalizer system, and its implementation on a commercial DSP.
4. Listening tests and conclusion.

## 2 Hi-fi car system model

Our target environment system is an audio system composed by a stereo audio source, an amplifier, a set of loudspeakers and the car cockpit, as sketched in fig. 1.

The audio source, the amplifier and the car cockpit can be considered linear with high approximation. In the following the non-linear behavior of loudspeakers will be neglected.

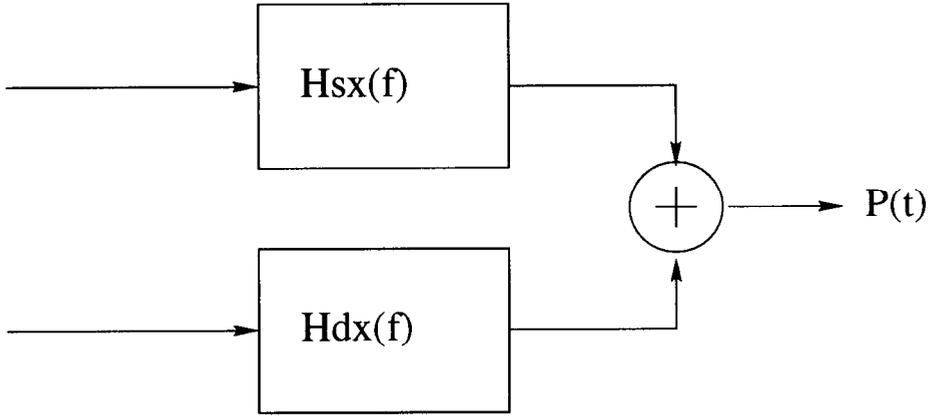


Figure 2: Linear model of the Hi-fi car system.

Therefore the whole sound reproduction chain can be considered a two-input one-output linear system, as sketched in fig. 2.

Under these assumptions the equalization of two single channels is equivalent to the equalization of the whole system. Therefore we will measure separately the two channels, in order to characterize their frequency response or their impulse response. Usually this kind of measurements are performed by means of MLS signals or sinusoidal signals sweeps [3]. The two methods produce satisfactory results with a few constraints. The number of sinusoidal signals used must be high and linearly increasing with frequency. A sweep of sinusoidal signals increasing exponentially with frequency would be more consistent with human hearing system, but though more effective to characterize low frequencies contents it would result in phase errors at higher frequencies.

If the digital method is used, the sampling frequency must of course be higher than  $F_{Nyquist}$  and the length of the MLS sequence must be consistent. These constraints are often automatically forced by the adopted tool.

### 3 Elaboration of measurement data

As reported the Aurora tool was used to to perform acoustic measurements of the audio reproduction system of a Fiat Lancia Delta. In the following data regarding the left channel are reported, without losing generality. The impulse response was obtained through an omnidirectional microphone mounted on a torso positioned in the driving position, see fig. 3. The microphone however is a diffuse-field type and thus smoothes heavily the high frequencies contents. The impulse response, whose duration is of about 50 ms, provides all the information concerning reflections, multiple path, ... i.e. all the events which affect the acoustic behavior of the system. The transformation of the inverse of the impulse response is reported in amplitude in figs. 4 and in fig. 5 as a function of time. In the following  $H_{inv}(f)$  will indicate the transformation of the inverse of the impulse response, and  $h_{inv}(n)$  the corresponding time-domain function. A standard sampling frequency of  $F_s = 44100 Hz$  will be considered and as usual “Tap” will indicate the number of non vanishing impulse response terms. Their time duration can be computed as  $L = \frac{Tap}{F_s}$ . As reported in fig. 5 the duration of  $h_{inv}(n)$  is of more than 8000 Taps, and thus it does not respect real-time constraints of a commercial DSP. Moreover the results obtained are not consistent with the desired shape, fig. 4. In this work the AD SHARC

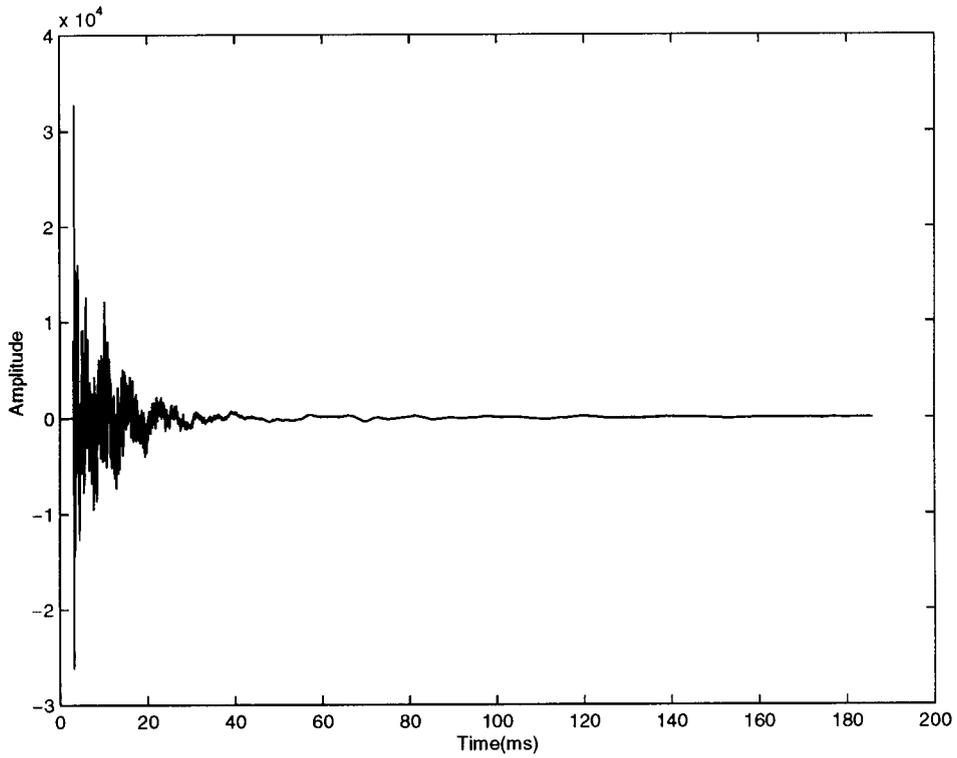


Figure 3: Impulse response of the left channel of a Fiat Lancia Delta (normalized data).

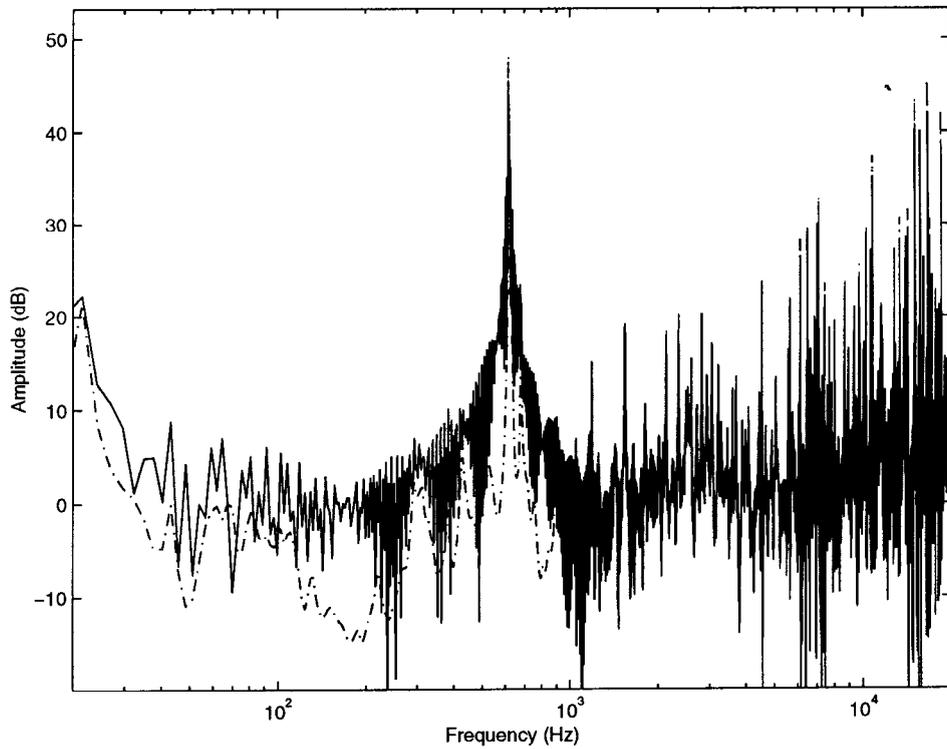


Figure 4: Amplitude of  $H_{inv}(f)$  (dashed), and the filter obtained with 8001 taps (solid).

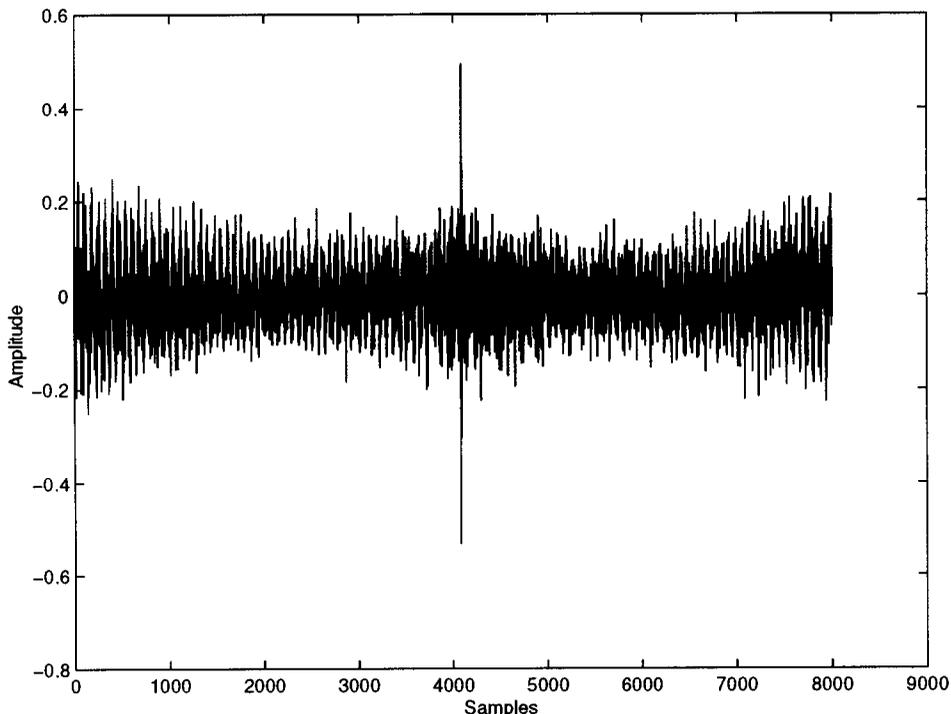


Figure 5: Impulse response of the synthesized filter (8001 taps).

DSP 21061 was used. It provides a computation power of around 40 Mips, with which 880 Taps can be computed for each sample at  $F_s = 44100\text{Hz}$ , respecting real-time constraints. Therefore this will be our constraint considering all the program overheads. Therefore the  $h_{inv}(n)$  is not directly implementable. Then a few approximation must be applied. Moreover it could be even dangerous to use an equalizing filter which employs the  $H_{inv}(f)$  directly. In fact psychoacoustic considerations on human earing system suggest the following items

1. An ideal flat band reproduction system is not necessarily pleasant. In general an increased low frequency response is desirable, especially as far as car-audio systems are concerned, where running car noises must be masked.
2. Human earing system resolution is logarithmic and limited at about one third of octave.

From these it stems that the target frequency response function should be not exactly flat, but consistent with some sort of tailored equalization response. This should be confirmed by listening test and by expert considerations, see fig. 6. From human earing resolution it stems that is ineffective to equalize all the frequency range with the same resolution. In fact at low frequencies the human earing system can tell between different sounds which are effectively near in frequency, while at high frequencies even the most sensitive ear fails. Therefore the equalization of very narrow peaks or holes in the frequency response would be inefficient and even unpleasant. Therefore to reproduce human earing resolution the inverse harmonic response  $H_{inv}(f)$  a median filter was applied [4] with a frequency window slightly shorter than a third of octave. These operations result in a new frequency response with reduced complexity, while the perceptual contents is almost unchanged, reported in fig. 7 compared with the measurements data. In order to achieve the target frequency response defined above, the  $H_{inv}$  processed by the median filter is multiplied by the target frequency response. Moreover an ideal equalizing

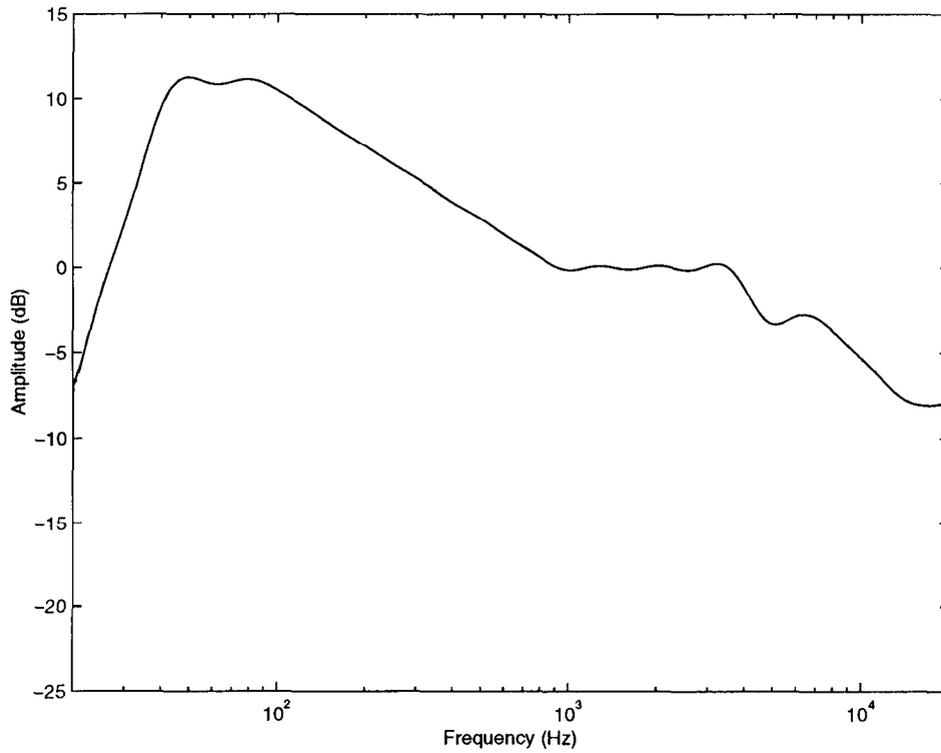


Figure 6: Desired frequency response.

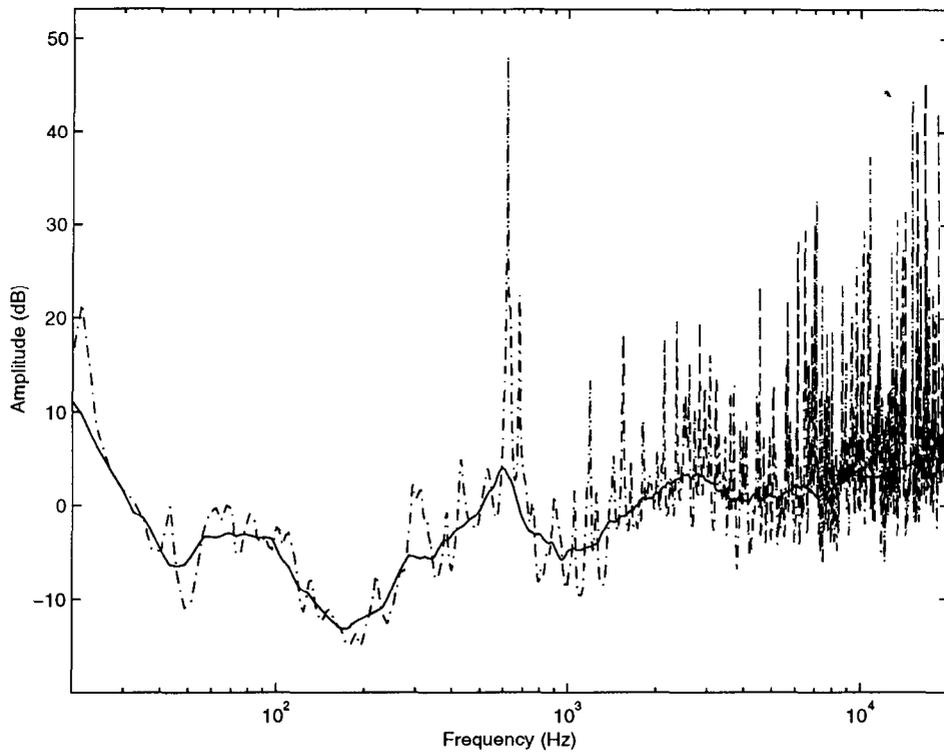


Figure 7: Amplitude of  $H_{inv}(f)$  (dashed), and its processed version (solid).

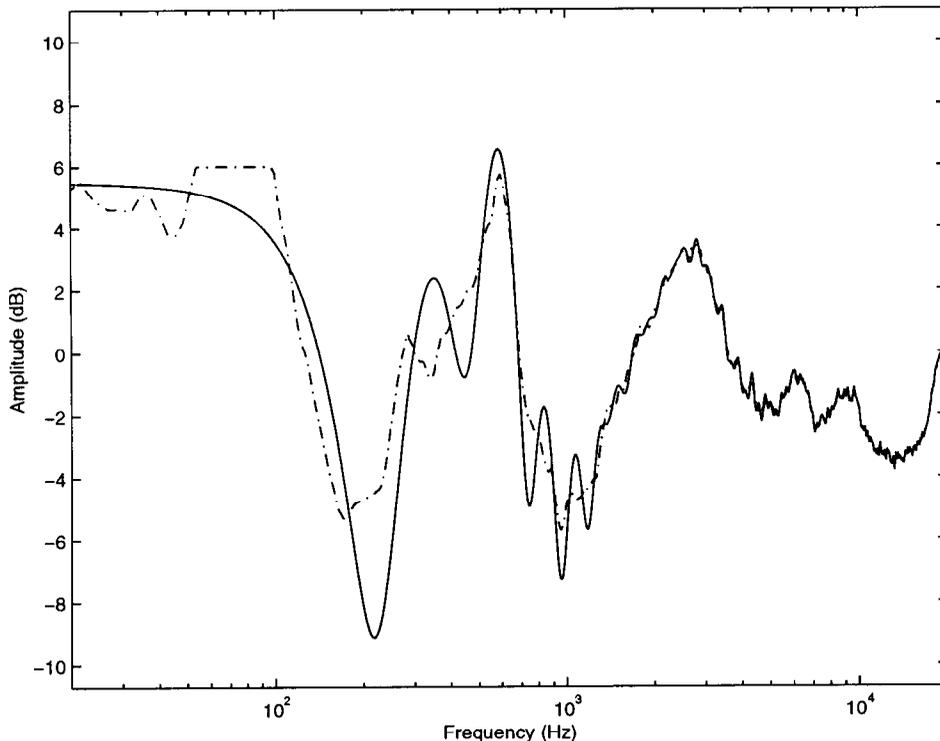


Figure 8: Harmonic response of the designed equalizer (Amplitude).

system should have a dynamic range of about  $30 \div 40dB$ . This means that the insertion of such a device before the amplifier could overcome the maximum allowable dynamics of the others devices, with a high possibility of arising distortion phenomena. To avoid this drawbacks it is necessary to limit the operating range for instance to  $\pm 6dB$ , so that the correction would be pleasant, smooth and natural. The shape of the filter which results after all the discussed elaborations is reported in fig. 8, and the number of its taps is of 401.

## 4 Architecture of the digital equalizer system

In the previous section measurements data have been elaborated in order to obtain an equalizer system, whose duration in Taps is reduced to 401. This would be consistent with the hardware limit of 880 taps/samples. But a better equalization can be achieved with a different processing scheme.

As an option fast hardware architecture could be employed to reduce the computational cost of the filter implementation, for instance overlap-save convolution techniques, but this is impractical because of the excessive amount of memory required with respect to the commonly available. The best trade-off was the adoption of a multi-rate architecture. In fact in a digital system no theoretical constraint exists, so that a single sampling frequency must be used. Therefore a generic audio signal whose frequency band is in the range  $[20Hz, 20KHz]$  can be split in two components, the former called  $x_{lp}(t)$  whose frequency band is  $[20Hz, \frac{F_s}{2N_{dec}}]$ , and the latter, partly overlapped, is called  $x_{hp}(t)$  whose frequency band is  $[\frac{0.8F_s}{2N_{dec}}, 20000Hz]$ . If we assume that it is possible to sample  $x_{lp}(t)$  at  $\frac{F_s}{N_{dec}}$ , and  $x_{hp}(t)$  at  $F_s$  we obtain the following advantages

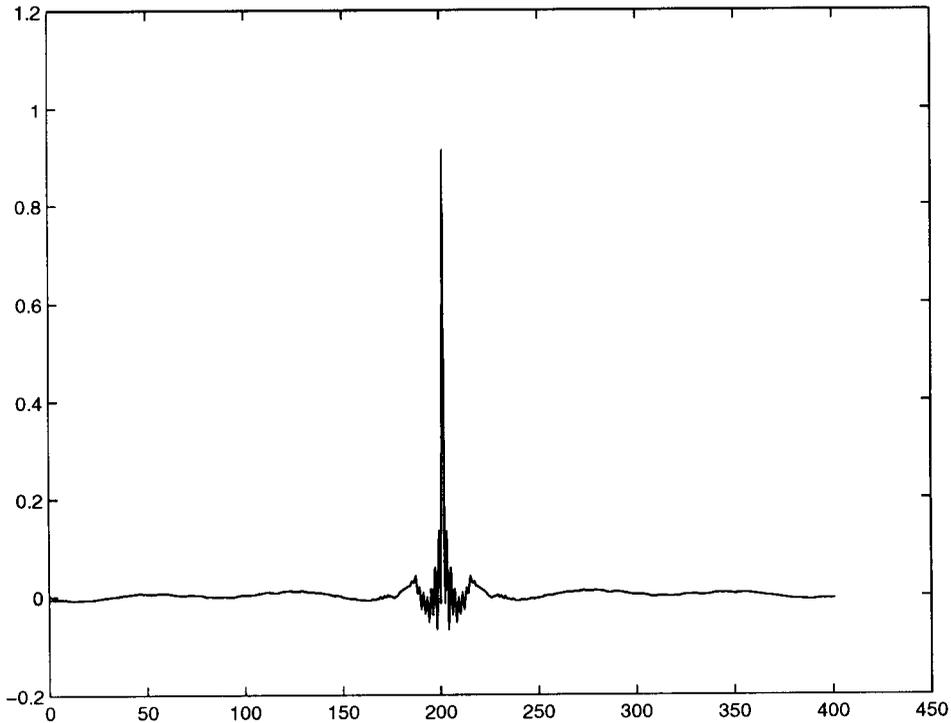


Figure 9: Impulse response of the designed equalizer.

- The complexity of the filter which operates on  $x_{hp}(n)$  is much lower than  $H_{inv}(f)$ , since its behavior below  $\frac{0.8F_s}{2N_{dec}}$  does not affect the signal.
- The signal  $x_{lp}(n)$  is operated at a sampling frequency  $N_{dec}$  times lower than  $F_s$ , and thus with a highly reduced cost.

The filters so obtained are defined  $h_{ilp}(n)$  and  $h_{ihp}(n)$ , and their length is of  $N_l = 155$  and  $N_h = 33$  Taps respectively. Moreover the sampling rate of the low-pass part is  $\frac{F_s}{N_{dec}}$ , and thus the effective cost of the processing is of  $\frac{N_l}{N_{dec}}$  Tap for each sample. The global cost is therefore  $\frac{N_l}{N_{dec}} + N_h$ , which in our examples is 59 Tap for each sample. In figs. 11, 10, 13 and 12 are reported the harmonic responses and the corresponding impulse responses of the above defined filters.

All the charts presented are defined unless of a constant phase, which results in a delay constant with frequency. However in order to obtain consistent processed data it is necessary to identify exactly the delay introduced by each processing stage. In the following the delays introduced by the two equalizing filters  $h_{ilp}$  and  $h_{ihp}$  are defined as  $N_{delay_{lp}}$  and  $N_{delay_{hp}}$  respectively. The choice adopted was that of FIR filters with linear phase, therefore the delay introduced by each of them is equal to  $(N - 1)/2$  Tap, where N the filter length.

#### 4.1 Multi-rate architecture

As described in the previous section it is necessary to split the signal in the two components  $x_{lp}(t)$ , and  $x_{hp}(t)$ , with band respectively  $[20, \frac{F_s}{2N_{dec}} Hz]$ ,  $[\frac{0.8F_s}{2N_{dec}}, 20000 Hz]$ . This can be obtained through a low-pass filter (LPF) with a cut-off frequency equal to  $\frac{0.8F_s}{2N_{dec}}$  and with its complementary high-pass filter (HPF) which can be implemented at no cost as in fig. 14. In order

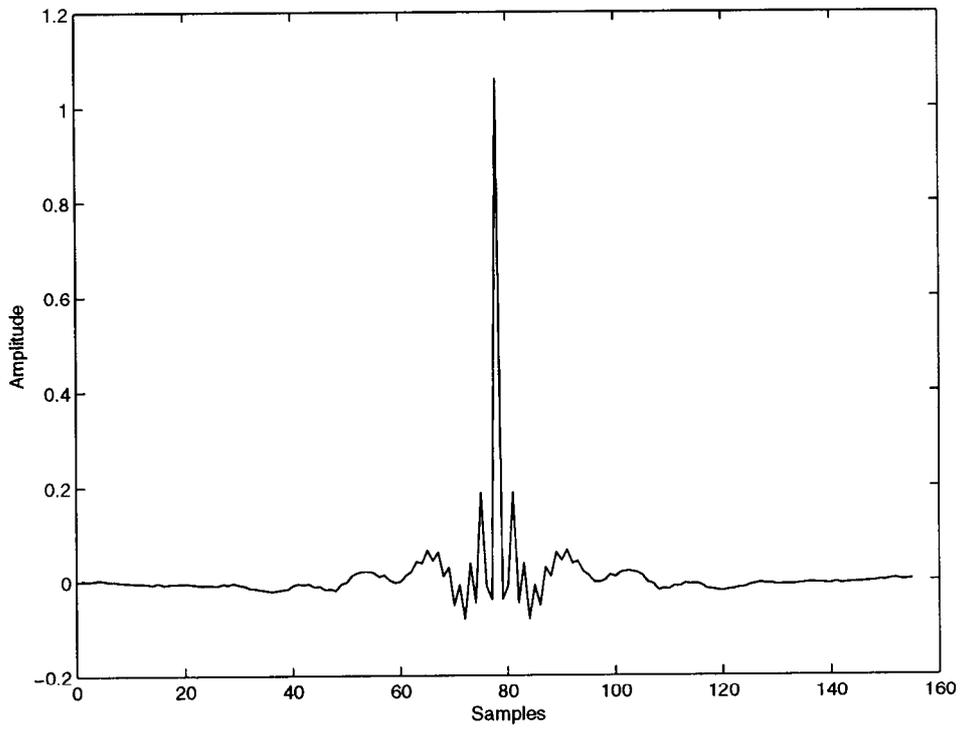


Figure 10: Impulse response of  $h_{ip}(n)$

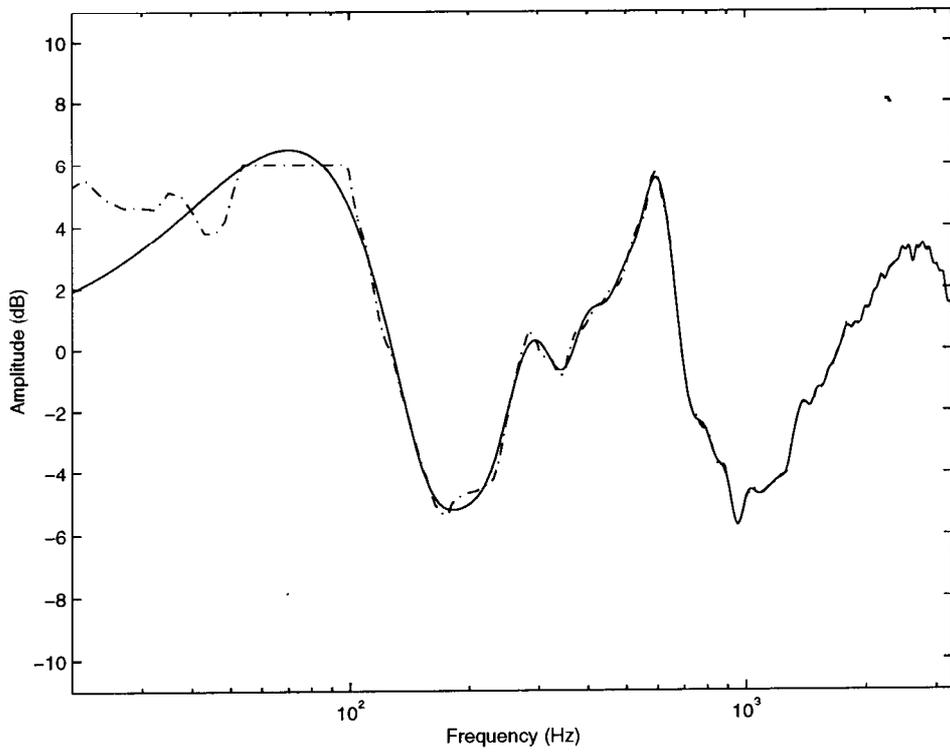


Figure 11: Amplitude of the system transfer function of  $h_{ip}(n)$

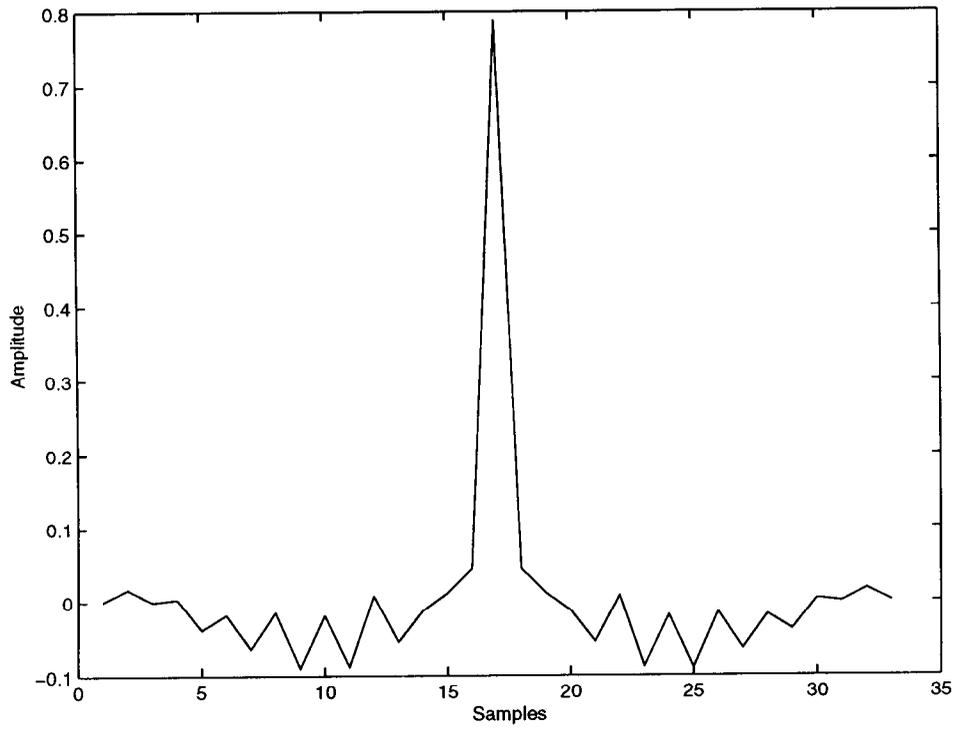


Figure 12: Impulse response of  $h_{ihp}(n)$

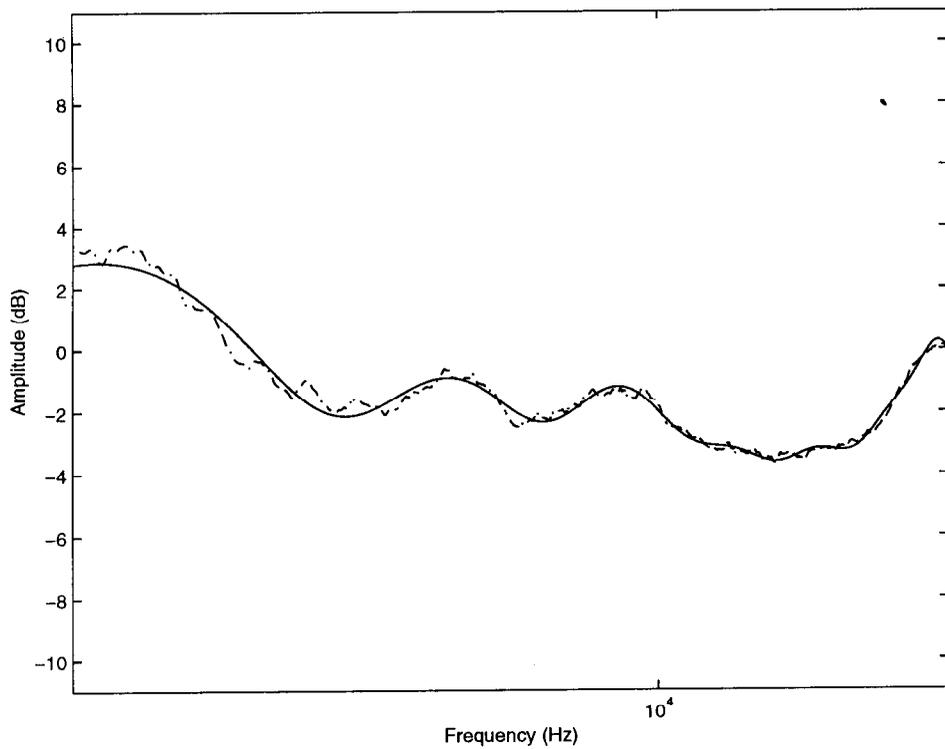


Figure 13: Amplitude of the system transfer function of  $h_{ihp}(n)$

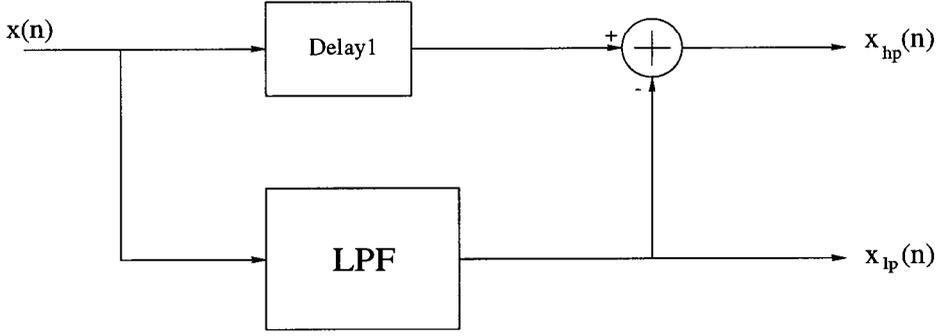


Figure 14: Block diagram of an digital crossover system.

to achieve two phased signal it is necessary to introduce a delay in the high-pass flow, and its delay is equal to  $\frac{N_{LPF}-1}{2}$ , i.e. the delay of the LPF filter.

Then the signal  $x_{lpF_s}(n)$  must be decimated with a factor  $N_{dec}$ , i.e. the sequence  $x_{lp}(n)$  is built, so that  $x_{lp}(n) = x_{lpF_s}(N_{dec}n)$ . The signal  $x_{lpF_s}(n)$  is affected by time-aliasing only if in its frequency spectrum appear components beyond  $\frac{F_s}{2N_{dec}}$ . In order to avoid aliasing is required that the LPF filter cuts more than  $80dB$  beyond the Nyquist frequency of the decimated signal.

Provided that  $y_{lp}(n)$  and  $y_{hp}(n)$  respectively are the equalized signals as in fig. 15, the reconstruction of the signal starts from the interpolation of  $y_{lp}(n)$ .

If we define a sequence sampled at  $F_s$  so that

$$z_{lp}(n) = \begin{cases} y_{lp}(m) & \text{when } n = mN_{dec} \\ 0 & \text{otherwise} \end{cases}$$

The frequency spectrum of  $z_{lp}(n)$  is given by

$$Z_{lp}(e^{j\omega}) = \sum_{n=-\infty}^{\infty} z_{lp}(n)e^{-j\omega n} = \sum_{m=-\infty}^{\infty} y_{lp}(m)e^{-j\omega N_{dec}m} = \quad (1)$$

$$= Y_{lp}(e^{j\omega N_{dec}}) \quad (2)$$

which can be interpreted as the periodic repetition of  $Y_{lp}(e^{j\omega})$  every  $\frac{F_s}{N_{dec}}$ , but sampled at  $F_s$  frequency. In order to retrieve the correct information of  $y_{lp}(n)$  an anti-aliasing filter must be applied. This low-pass filter is called  $LPF_2$  and must comply with the following constraints

- It must be a flat filter in the band of  $y_{lp}(n)$ , i.e. in that frequency range where  $LPF$  is higher than  $-20dB$ ;
- The fading beyond  $\frac{F_s}{2N_{dec}}$  must be higher than  $80dB$ .
- The gain of  $LPF_2$  must be  $N_{dec}$  in order to compensate the energy loss due to the interpolation process.

Since the  $z_{lp}(n)$  sequence is significative only each  $N_{dec}$  samples the computation of  $LPF_2$  can be simplified accounting only for significative terms. Namely

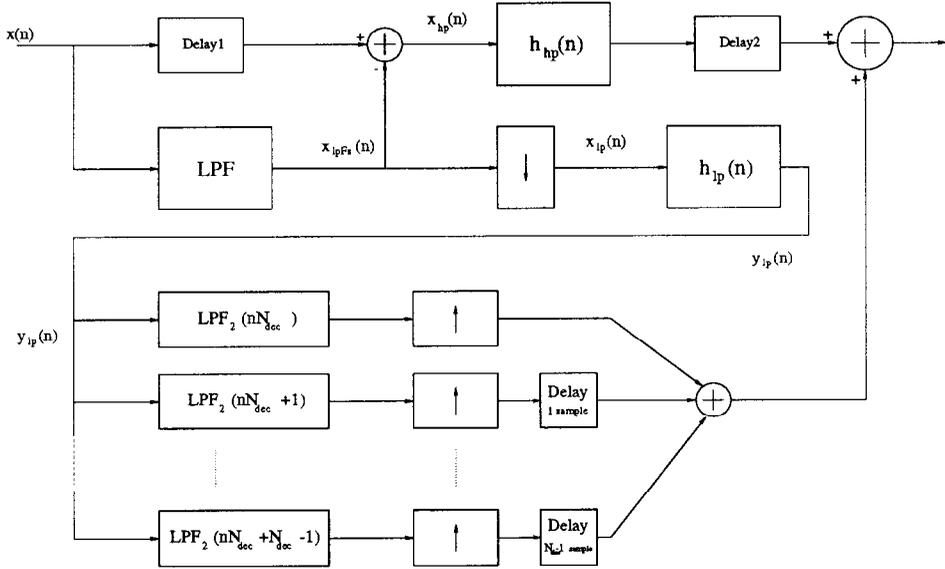


Figure 15: Block diagram of the multi-rate equalizer architecture.

$$z_{lp}(n) \star LPF_2 = \begin{cases} y_{lp}(n) \star LPF_2(nN_{dec}) & \text{if } n = mN_{dec} \\ y_{lp}(n) \star LPF_2(nN_{dec} + 1) & \text{if } n = mN_{dec} + 1 \\ y_{lp}(n) \star LPF_2(nN_{dec} + N_{dec} - 1) & \text{if } n = mN_{dec} + N_{dec} - 1 \end{cases}$$

Where  $\star$  stands for the convolution operator, and each convolution can be implemented with filters whose length is  $\frac{1}{N_{dec}}$  than expected. The architecture depicted in fig. 15 is thus obtained.

The anti-aliasing filters consistent with the above defined constraints, whose length is 181 for  $LPF$  and 341 for  $LPF_2$ , are implemented with two Kaiser windows. In figs. 16, 17, 18, 19, 20 are reported their time and frequency behavior. Every filter is synthesized with even symmetry and with an odd number of taps. Therefore their phase is perfectly linear as a function of frequency, and the delay introduced by each filter is exactly  $\frac{N_{tap}-1}{2}$ .

## 5 Conclusion

The equalizer structure described in the previous sections was implemented in assembly on a 21061 EZ-LITE DSP board, and the software tools of Matlab [5] were used to synthesize the suitable filters. A Fiat Lancia Delta was characterized and used as a target with the insertion of the audio equalizer. The direct measurements of the only amplitude equalizer are reported in fig. 21 e 22 and its amplitude characteristics is in fig. 23. We can stem from them that the phase is perfectly linear unless a slight distortion introduced by A/D and D/A converters.

Listening tests as well as distortion measures confirm that the equalization task can be achieved, and that a subjective improvement of sound quality can be obtained. The main impacts of equalization are the nice balancing of sounds coming from different instruments, and the increase of low frequencies, an option which is necessary to compensate running car noise, as resulted from experience. Moreover the virtual source of sound is shifted from the doors, where loudspeaker are, so that the listener perceives a frontal audio source, and a more natural

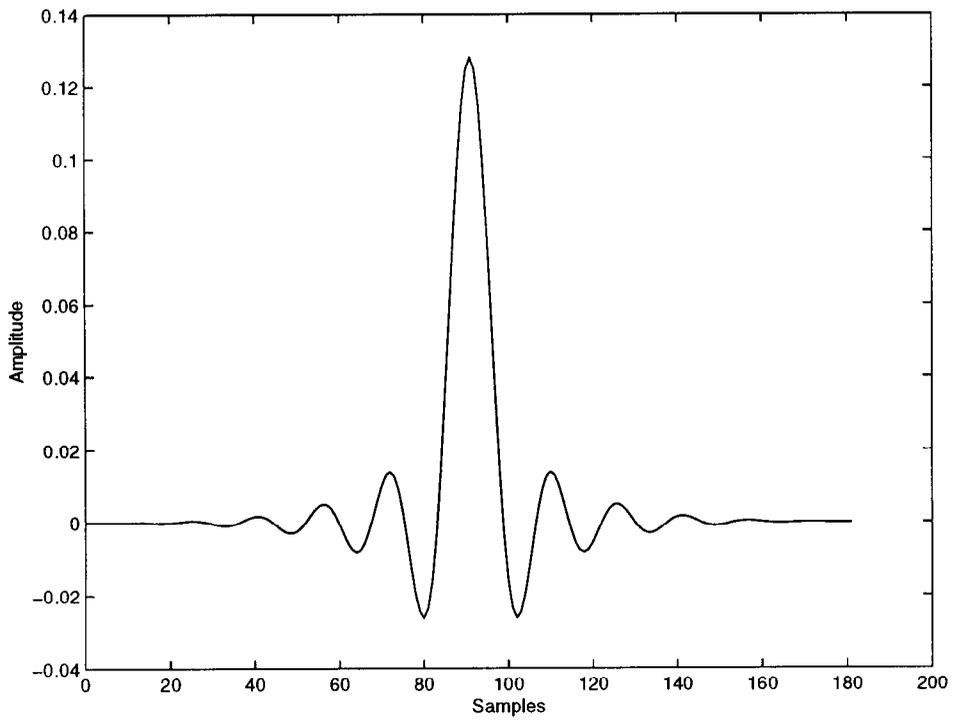


Figure 16:  $lpf(n)$

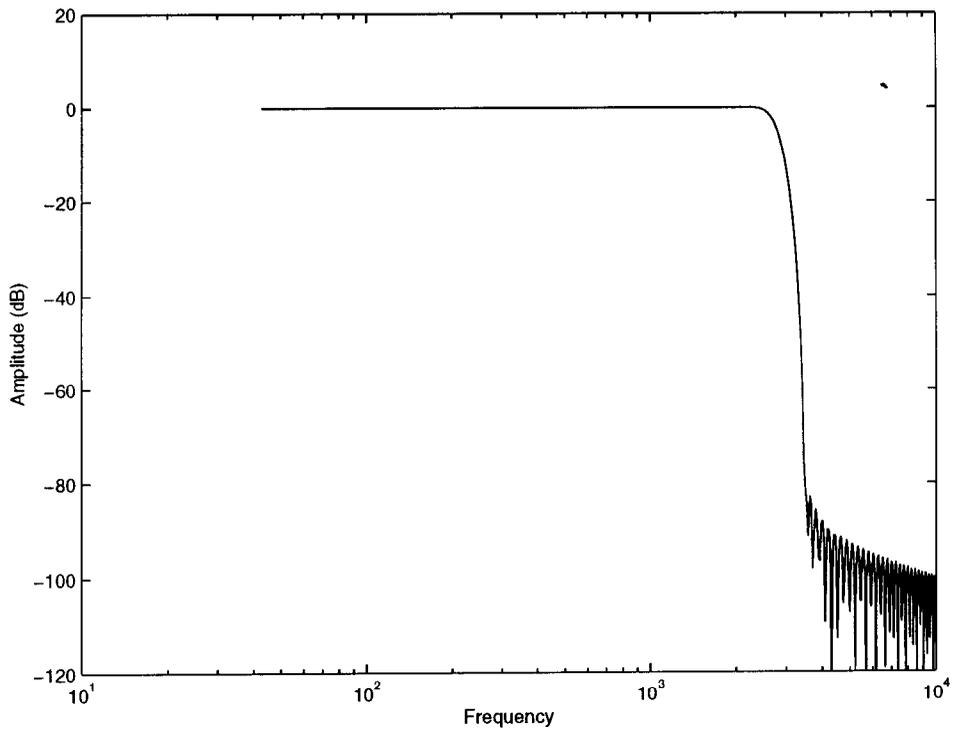


Figure 17:  $LPF(f)$

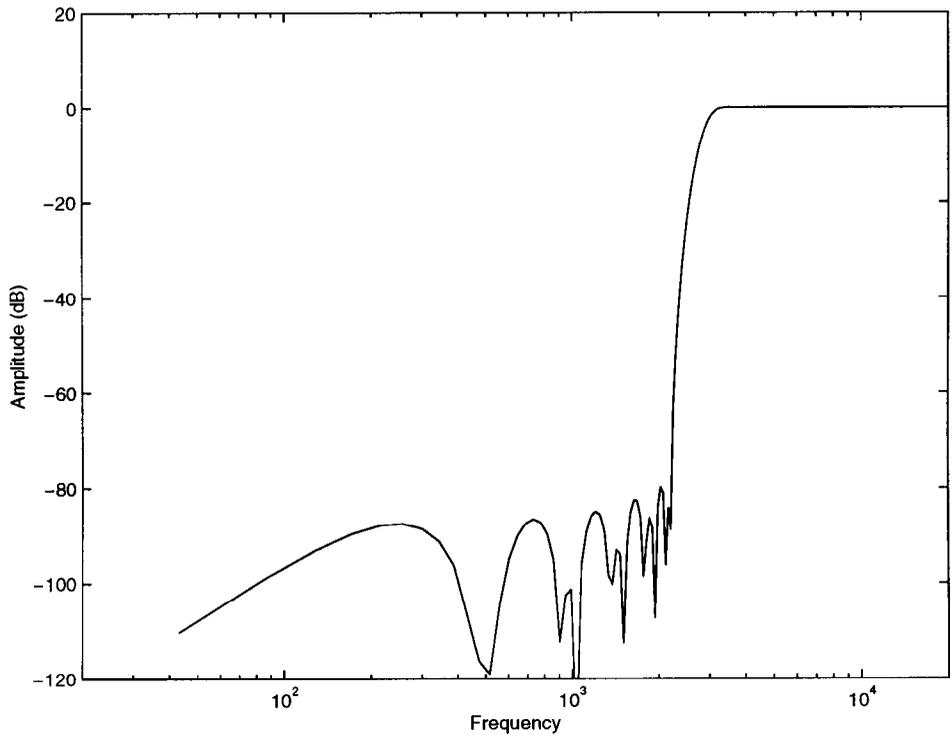


Figure 18:  $HPF(f)$

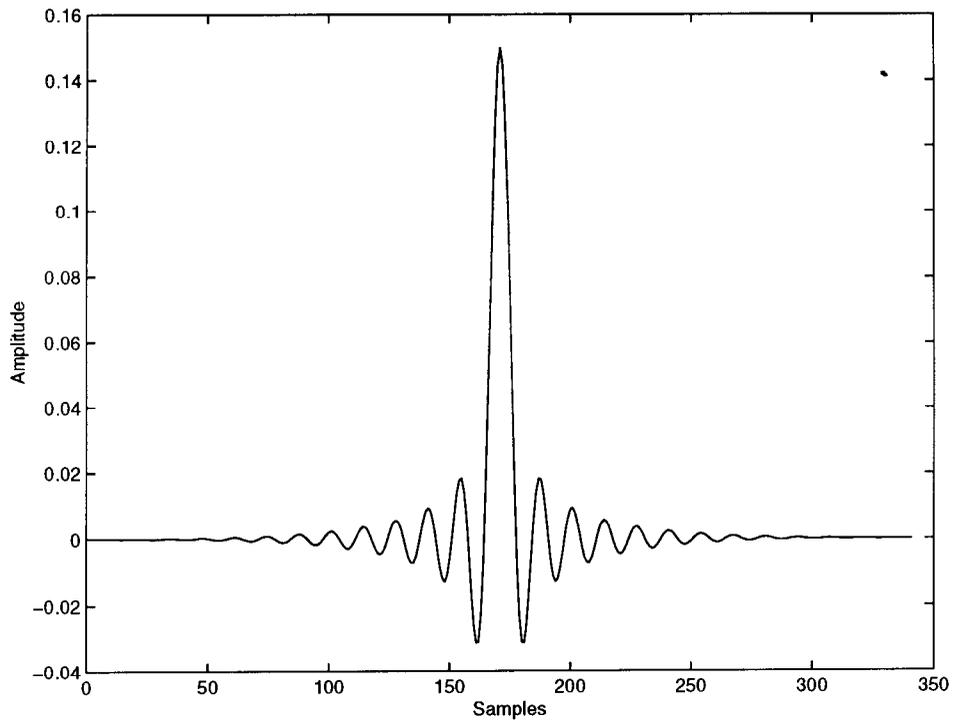


Figure 19:  $lpf_2(n)$

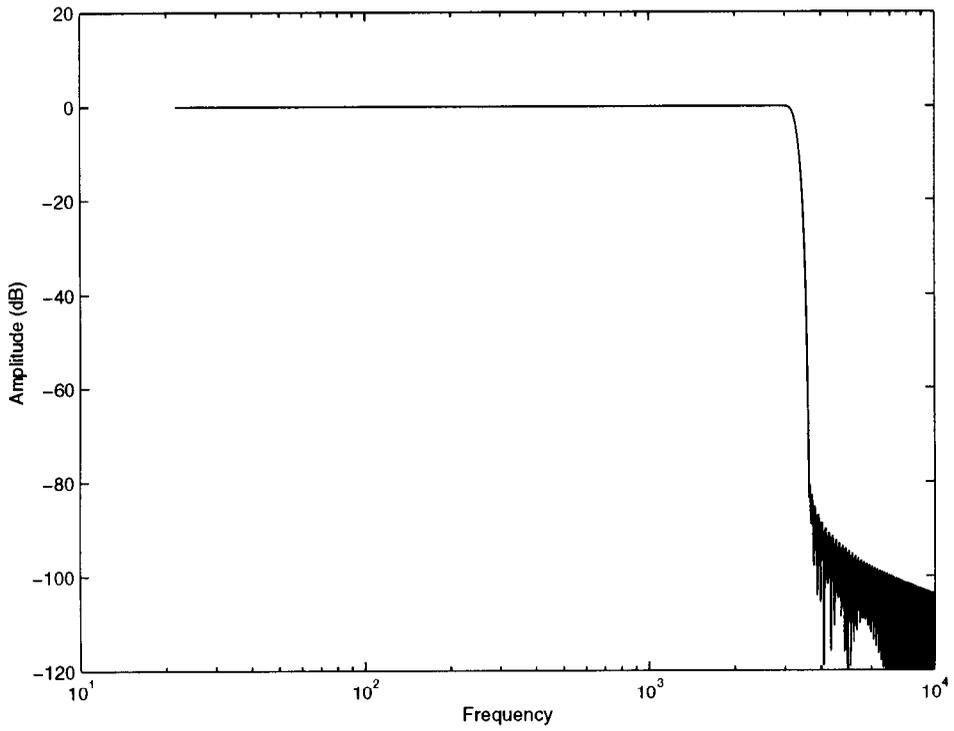


Figure 20:  $LPF_2(f)$

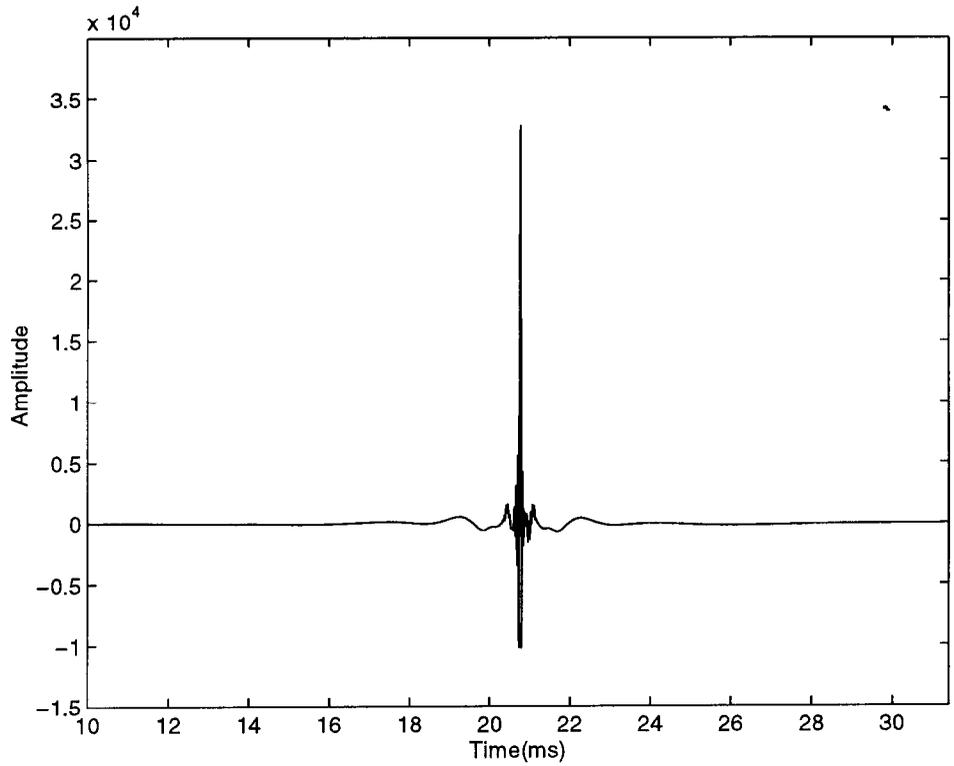


Figure 21: Impulse response of the multi-rate equalizer.

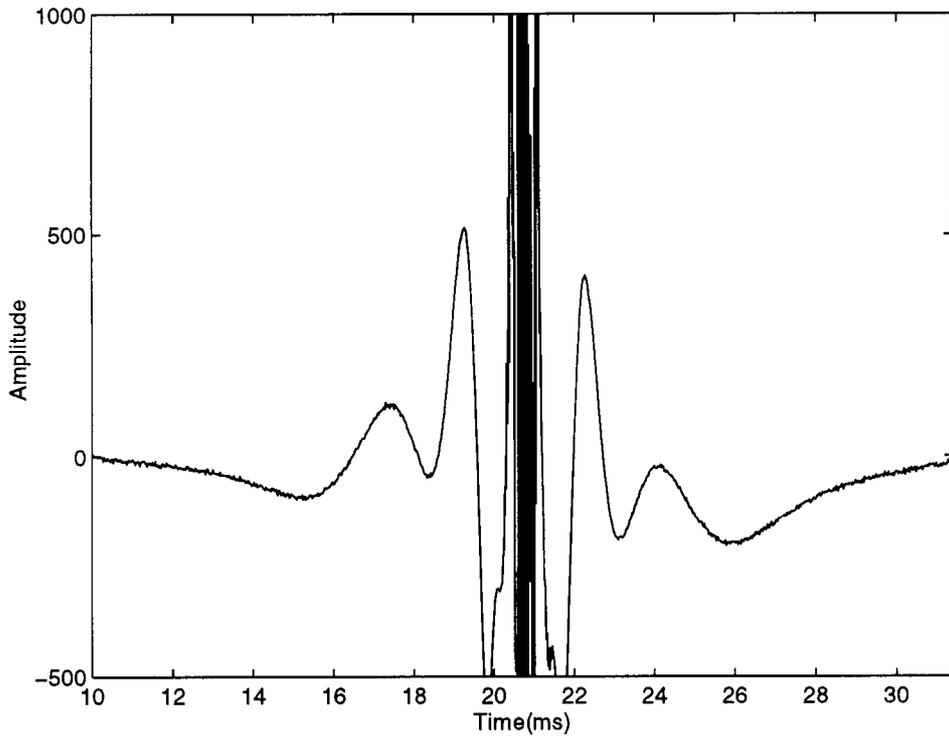


Figure 22: Impulse response of the multi-rate equalizer (detail).

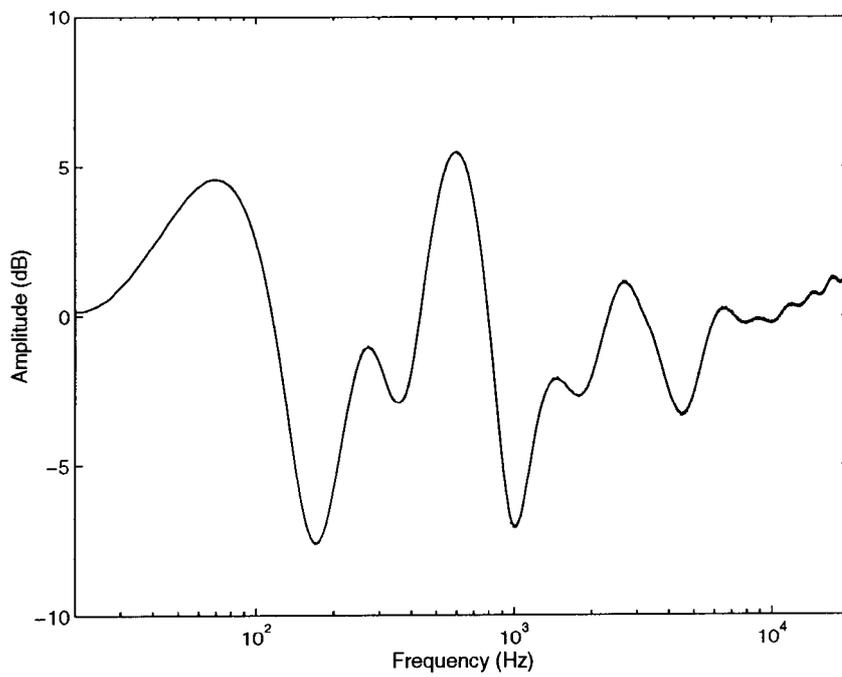


Figure 23: Frequency response of the multi-rate equalizer (Amplitude).

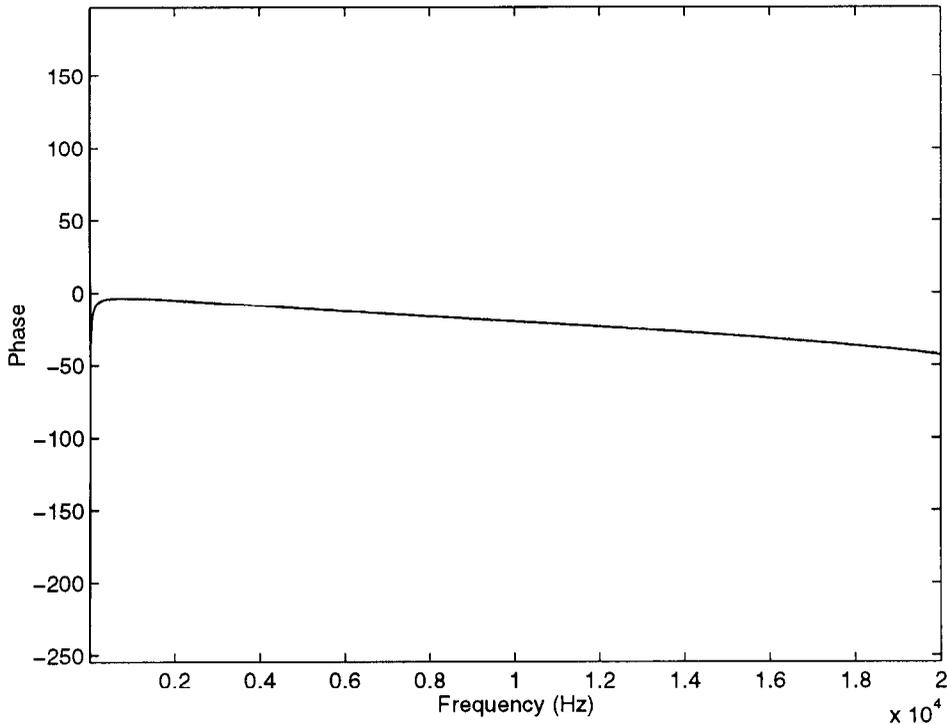


Figure 24: Frequency response of the multi-rate equalizer (Amplitude).

and pleasant sound. A 70 taps delay introduced in the left channel is also very useful to improve the sound image for a listener in the driver position and does not affect the others. The equalization system seems robust with respect to the listener position and different measures in different points produce the same shape in amplitude but different phase. Due to the limitation of the used microphone the target shape was compensated adding  $4 \div 6dB$  beyond  $4KHz$ , thus we can still consider that diffuse-field microphones affect the effectiveness of the equalization. In conclusion we can observe that

- A digital system acting on third of octave can be effective within a car cockpit as an equalization system.
- The proposed system can be implemented on commercial low cost DSP based boards.
- The converters available introduced a critical noise and dynamic range reduction. A better option would be that of inserting the proposed equalizer structure in the car radio before amplifier and volume control with neglectable conversion noise (i.e. less than 80dB).
- A delay introduced in the left channel improves sound image for the driver.
- The equalizer system proves to be robust and effective at each position of car passengers.
- The proposed architecture features only amplitude equalization. This option is a fine trade-off between computational cost and subjective results. In fact, so doing we can achieve a fine equalization and the multi-rate architecture allows to implement the filters on a single AD 21061 EZ-LITE for both stereo channels. Moreover the correction of the

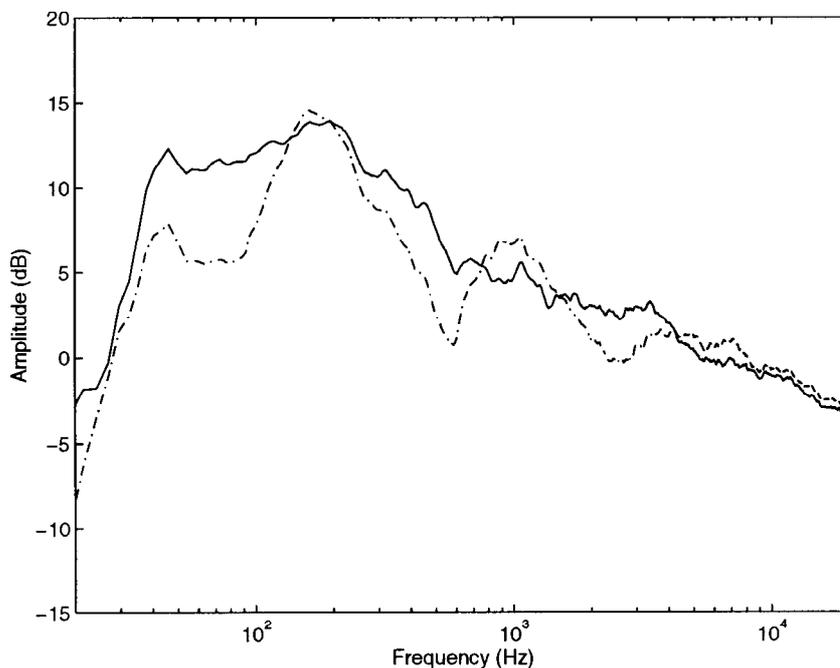


Figure 25: SPL of the left channel measured with (solid line) and without equalizer (dashed line).

phase would be still possible, simply by changing the tool of filter synthesis, but proves to produce a slight increase of sound quality, if any.

In figs. 26 and 26 are reported the SPL curves measured within a standard Lancia Delta cockpit, after the proposed equalization.

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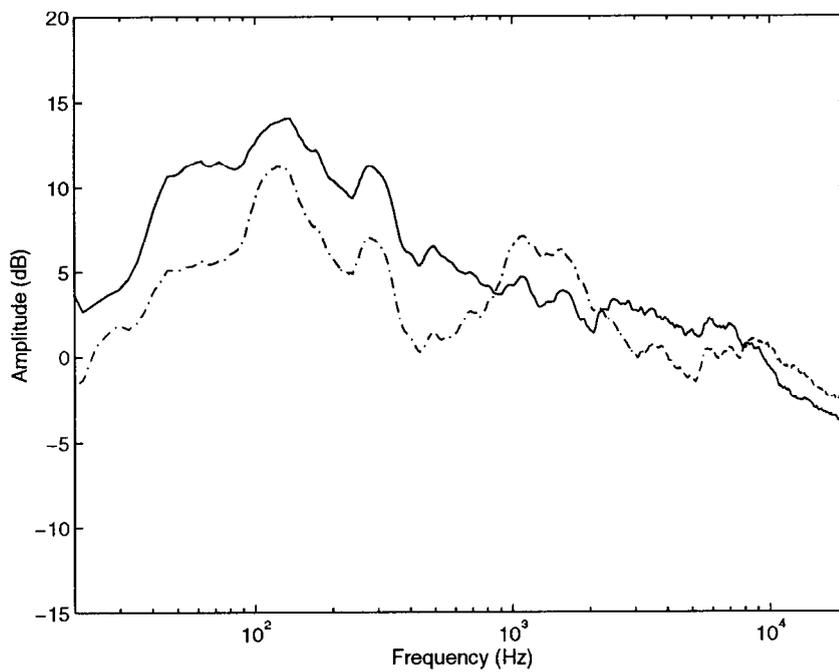


Figure 26: SPL of the right channel measured with (solid line) and without equalizer (dashed line).

[4] S.K.Mitra and J.F.Kaiser, *Handbook of digital signal processing*, McGraw-Hill, New-York, 1993.

[5] The Mathworks, Inc., *Signal Processing Toolbox*, 1998.